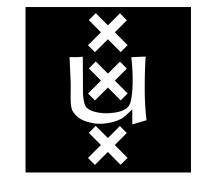




Causality-inspired ML: what can causality do for ML?

Sara Magliacane

University of Amsterdam MIT-IBM Watson Al Lab





- Real-world ML needs to deal with:
 - Biased data (fairness, selection bias, generalization)
 - Heterogeneous data, small samples, missing/corrupted data, not iid
 - Actionable insights (decisions cannot be made on correlations)

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graph

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- Transfer learning:
 - How can I predict what happens when the distribution changes?





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- Transfer learning:
 - How can I predict what happens when the distribution changes?









- Causal inference:
 - How can I predict what happens when the distribution changes after an intervention?
 - Perfect intervention: do-calculus [Pearl, 2009]
 - X is independent of its parents
 - Soft intervention on X:
 - Change of P(X) parents)

Transfer learning:

 How can I predict what ha when the distribution chan

Very general - can model also changes in distribution that are not from "real" interventions





[Pe 1, 2009]







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Transfer learning:

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Changes in company of the changes in the chang

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[Pe 1, 2009]

X is independent of its parents







- Soft intervention on X:
 - Change of P(X| parents)

Not a new idea!

On Causal and Anticausal Learning

ICML 2012

Bernhard Schölkopf, Dominik Janzing, Jonas Peters, Eleni Sgouritsa, Kun Zhang

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Joris Mooij

J.MOOIJ@CS.RU.NL

Institute for Computing and Information Sciences, Radboud University, Nijmegen, The Netherlands

Abstract

We consider the problem of function estimation in the case where an underlying causal model can be inferred. This has implications for popular scenarios such as covariate shift, concept drift, transfer learning and semi-supervised learning. We argue that causal knowledge may facilitate some approaches for a given problem, and rule out others. In particular, we formulate a hypothesis for when semi-supervised learning can help, and corroborate it with empirical results.

for causal inference in the machine learning community.

An example illustrating the difference between the statistical and the causal point of view is the correlation between the frequency of storks and the human birth rate (Matthews, 2000). We may be able to train a good predictor of the birth rate which uses the frequency of storks (along with other features) as an input. However, if politicians asked us whether one could boost the birth rate by increasing the number of storks, we would have to tell them that this kind of *intervention* is not covered by the standard i.i.d. assumption of statistical learning. In practice, however, interventions can be relevant, distributions may shift over time, and we might want to combine data recorded under different

Causality allows us to reason systematically about distribution shifts

On Causal and Anticausal Learning

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J. R. Statist. Soc. B (2016) 78, Part 5, pp. 947-1012

Causal inference by using invariant prediction: identification and confidence intervals

Jonas Peters

Max Planck Institute for Intelligent Systems, Tübingen, Germany, and Eidgenössiche Technische Hochschule Zürich, Switzerland

and Peter Bühlmann and Nicolai Meinshausen Eidgenössiche Technische Hochschule Zürich, Switzerland

Domain Adaptation as a Problem of Inference on Graphical Models

Kun Zhang^{1*}, Mingming Gong^{2*}, Petar Stojanov³ Biwei Huang¹, Qingsong Liu⁴, Clark Glymour¹

Department of philosophy, Carnegie Mellon University ² School of Mathematics and Statistics, University of Melbourne ³ Computer Science Department, Carnegie Mellon University, ⁴ Unisound AI Lab kunz1@cmu.edu, mingming.gong@unimelb.edu.au, liuqingsong@unisound.com {pstojano, biweih, cg09}@andrew.cmu.edu

Anchor regression: heterogeneous data meet causality

Dominik Rothenhäusler, Nicolai Meinshausen, Peter Bühlmann and Jonas Peters

Invariant Risk Minimization

Invariant Models for Causal Transfer Learning

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Department of Engineering Univ. of Cambridge, United Kingdom

Bernhard Schölkopf

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Invariance, Causality and Robustness

2018 Neyman Lecture *

Peter Bühlmann Seminar for Statistics, ETH Zürich

Counterfactual Invariance to Spurious Correlations: Why and How to Pass Stress Tests

Victor Veitch^{1,2}, Alexander D'Amour¹, Steve Yadlowsky¹, and Jacob Eisenstein¹

> ¹Google Research ²University of Chicago

Domain Adaptation by Using Causal Inference to Predict Invariant Conditional Distributions

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IBM Research* sara.magliacane@gmail.com Thijs van Ommen

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A Causal View on Robustness of Neural Networks

Cheng Zhang

Microsoft Research Cheng.Zhang@microsoft.com

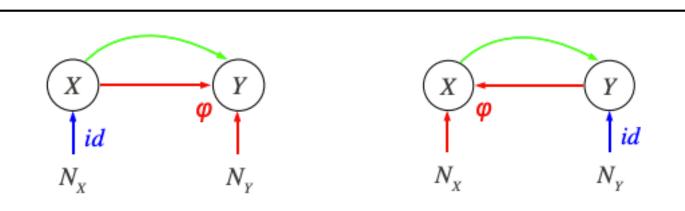
Kun Zhang Yingzhen Li * Carnegie Mellon University Microsoft Research kunz1@cmu.edu Yingzhen.Li@microsoft.com

and many many more....

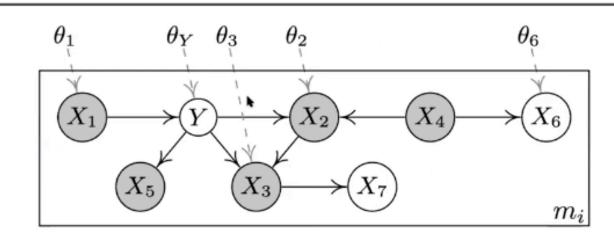
Martin Arjovsky, Léon Bottou, Ishaan Gulrajani, David Lopez-Paz

Causality allows us to reason systematically about distribution shifts, e.g. through graphs

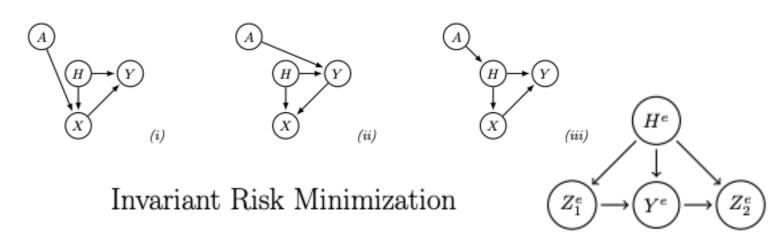
On Causal and Anticausal Learning



Domain Adaptation as a Problem of Inference on Graphical Models

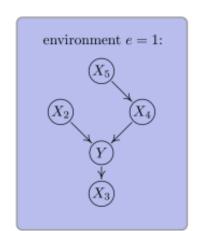


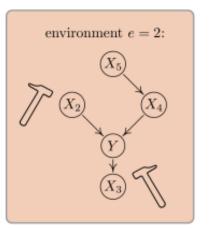
Anchor regression: heterogeneous data meet causality

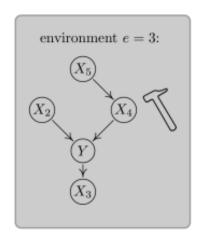


J. R. Statist. Soc. B (2016) 78, Part 5, pp. 947–1012

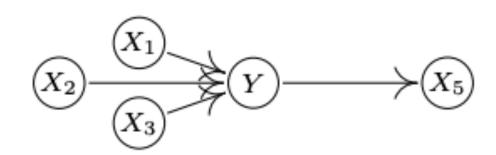
Causal inference by using invariant prediction: identification and confidence intervals



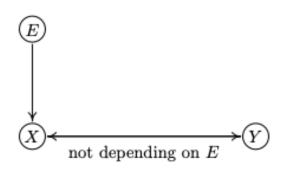




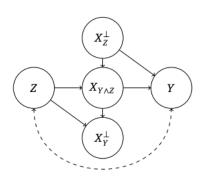
Invariant Models for Causal Transfer Learning

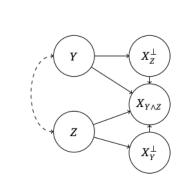


Invariance, Causality and Robustness

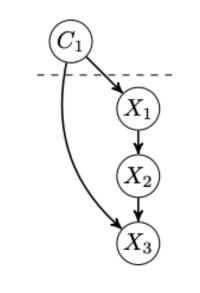


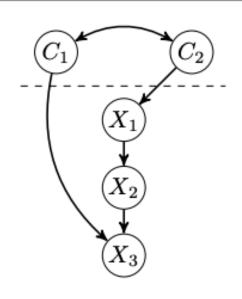
Counterfactual Invariance to Spurious Correlations: Why and How to Pass Stress Tests



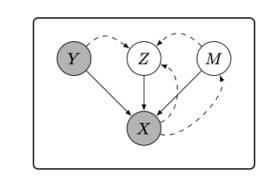


Domain Adaptation by Using Causal Inference to Predict Invariant Conditional Distributions





A Causal View on Robustness of Neural Networks



and many more....

Causality allows us to reason systematically about distribution shifts, e.g. through graphs

On Causal and Anticausal Learning

Learning

J. R. Statist. Soc. B (2016) **78**, Part 5, pp. 947–1012

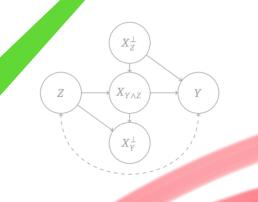
Even if unknown

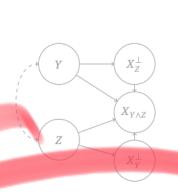
asing invariant prediction:

at e = 2: X_{5} Y X_{4} Y X_{3}

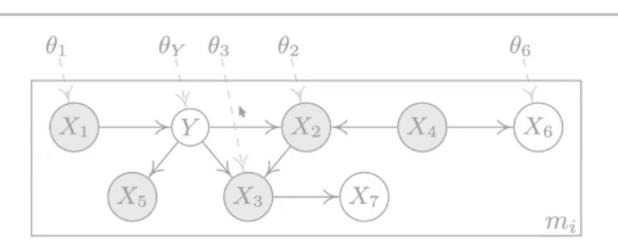


Counterfactual Levariance to Spurious Correlations: Why and How to Pass Stress Tests

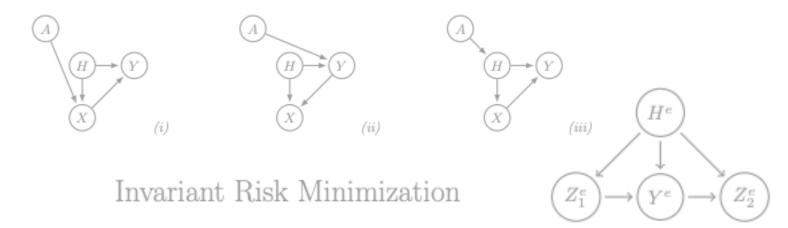




Domain Adaptation as a Problem of Inference on Graphical Models



Anchor regression: heterogeneous data meet causality



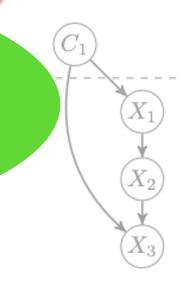
Even if we are in a zero-shot setting

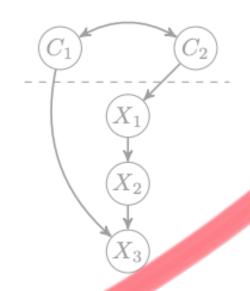


Invariance, Causality and Robustness

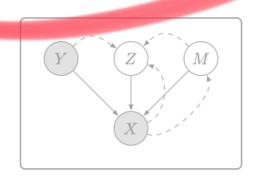


Domain Adaptation by Using Causal Inference to Predict Invariant Conditional Distributions





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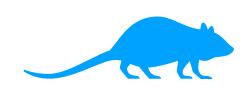


and many more....

Unsupervised multi-source domain adaptation

		X1	X2	Y	
	Normal	0.1	2	0	
	Normal	0.2	3	0	Source domain
	Normal	1.1	2	1	
	Normal	0.1	3	0	
					_
_		X1	X2	Y	
	Gene A	X1 3.1	X2 2	Y ?	
	Gene A Gene A			_	Target domain
		3.1	2	?	Target domain
	Gene A	3.1	2	?	Target domain No labels in target

• Estimate \hat{f} in Y = $\hat{f}(\mathbf{X})$ from source domains and by exploiting the knowledge of the change from the unlabelled data in target



	X1	X2	Y
Normal	0.1	2	0
Normal	0.2	3	0
Normal	1.1	2	1
Normal	0.1	3	0



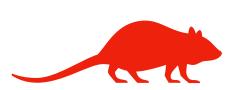


	X1	X2	Y
Gene A	3.1	2	?
Gene A	3.2	3	?
Gene A	4	2	?
Gene A	3.2	3	?



D	X1	X2	Y
Normal	0.1	2	0
Normal	0.2	3	0
Normal	1.1	2	1
Normal	0.1	3	0





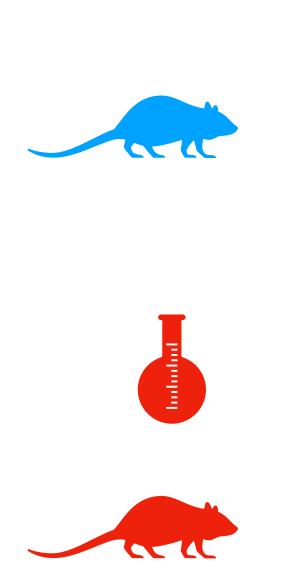
D	X 1	X2	Y
Gene A	3.1	2	?
Gene A	3.2	3	?
Gene A	4	2	?
Gene A	3.2	3	?

Add a variable D to represent the domain

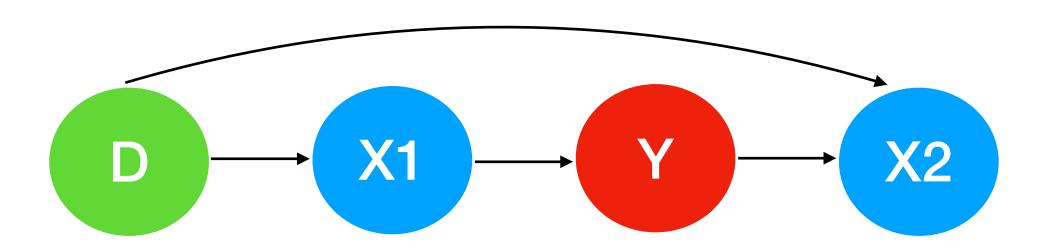
Imminimi

D	X1	X2	Y
Normal	0.1	2	0
Normal	0.2	3	0
Normal	1.1	2	1
Normal	0.1	3	0
Gene A	3.1	2	?
Gene A	3.2	3	?
Gene A	4	2	?
Gene A	3.2	3	?

- Add a variable D to represent the domain
- Consider the data as coming from a single distribution P(X,Y, D)



D	X1	X2	Y
Normal	0.1	2	0
Normal	0.2	3	0
Normal	1.1	2	1
Normal	0.1	3	0
Gene A	3.1	2	?
Gene A	3.2	3	?
Gene A	4	2	?
Gene A	3.2	3	?

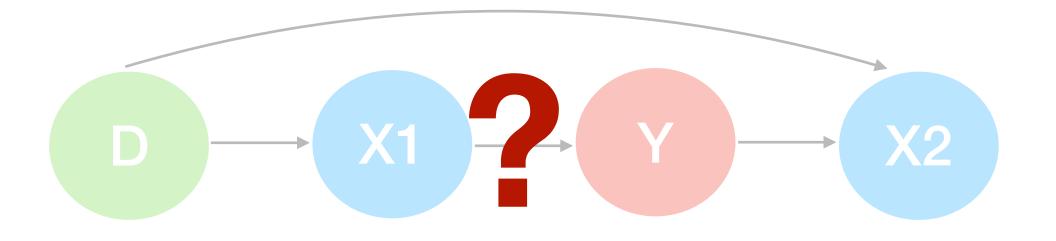


 We can represent P(X,Y, D) with a (possibly unknown) causal graph

- Add a variable D to represent the domain
- Consider the data as coming from a single distribution P(X,Y, D)

- Industrial

D	X1	X2	Y
Normal	0.1	2	0
Normal	0.2	3	0
Normal	1.1	2	1
Normal	0.1	3	0
Gene A	3.1	2	?
Gene A	3.2	3	?
Gene A	4	2	?
Gene A	3.2	3	?



 We can represent P(X,Y, D) with a (possibly unknown) causal graph

Add a variable D to represent the domain

We can still use d-separations/ conditional independences to reason about invariances

• Consider the data as coming from a single distribution P(X,Y, D)

Structural causal model - domain/environment variable

$$\begin{cases} \epsilon_1, \epsilon_2, \epsilon_3, \epsilon_Y \sim \mathcal{N}(0, 1) \\ X_1 = 10 + \epsilon_1 \\ Y = 3X_1 + \epsilon_Y \end{cases} D = 0$$

$$X_2 = -2Y + \epsilon_2$$

$$X_3 = 2Y + 0.1\epsilon_3$$

$$\begin{cases} \epsilon_1, \epsilon_2, \epsilon_3, \epsilon_Y \sim \mathcal{N}(0, 1) \\ X_1 = 10 + \epsilon_1 \\ Y = 3X_1 + \epsilon_Y \end{cases} D = 1$$

$$\begin{cases} X_2 = 1 \\ X_3 = 2Y + 0.1\epsilon_3 \end{cases}$$

$$\begin{cases} \epsilon_1, \epsilon_2, \epsilon_3, \epsilon_Y \sim \mathcal{N}(0,1) \\ X_1 = 10 + \epsilon_1 \\ Y = 3X_1 + \epsilon_Y \end{cases}$$

$$X_2 = 10Y + \epsilon_Y$$

$$X_3 = 2Y + 0.1\epsilon_3$$

$$\begin{cases} \epsilon_1, \epsilon_2, \epsilon_3, \epsilon_\gamma \sim \mathcal{N}(0,1) \\ X_1 = 10 + \epsilon_1 \\ Y = 3X_1 + \epsilon_Y \end{cases}$$

$$X_2 = \begin{cases} -2Y + \epsilon_2 \text{ if } D = 0 \\ 1 & \text{if } D = 1 \\ 10Y + \epsilon_Y \text{ if } D = 2 \end{cases}$$

$$X_3 = 2Y + 0.1\epsilon_3$$

Domain adaptation example

$$\begin{cases} \epsilon_1, \epsilon_2, \epsilon_3, \epsilon_Y \sim \mathcal{N}(0, 1) \\ X_1 = 10 + \epsilon_1 \\ Y = 3X_1 + \epsilon_Y \\ X_2 = -2Y + \epsilon_2 \\ X_3 = 2Y + 0.1\epsilon_3 \end{cases}$$

$$\begin{cases} \epsilon_1, \epsilon_2, \epsilon_3, \epsilon_Y \sim \mathcal{N}(0, 1) \\ X_1 = 10 + \epsilon_1 \\ Y = 3X_1 + \epsilon_Y \end{cases}$$
$$X_2 = 1$$
$$X_3 = 2Y + 0.1\epsilon_3$$

obs

Source domains

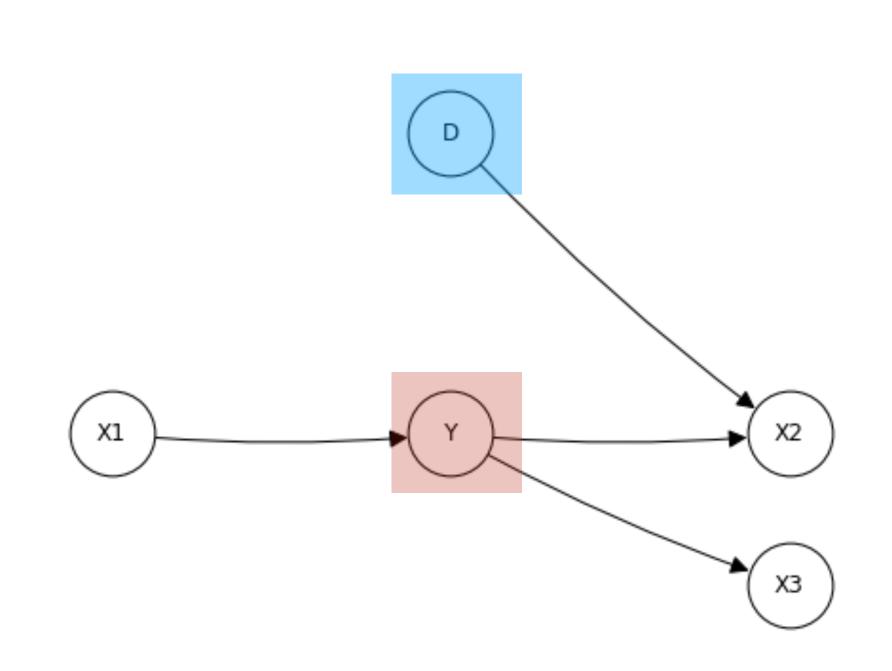
$$do(X_2 = 1)$$

$$\begin{cases} \epsilon_{1}, \epsilon_{2}, \epsilon_{3}, \epsilon_{Y} \sim \mathcal{N}(0,1) \\ X_{1} = 10 + \epsilon_{1} \\ Y = 3X_{1} + \epsilon_{Y} \end{cases}$$

$$X_{2} = 10Y + \epsilon_{Y}$$

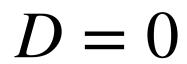
$$X_{3} = 2Y + 0.1\epsilon_{3}$$

$$do(X_{2} = f'_{2}(Y, \epsilon_{X_{2}}))$$
Target domain

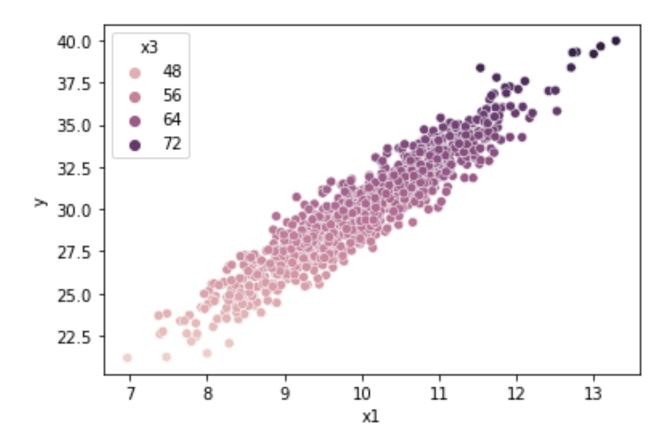


Domain adaptation example - X1

P(Y|X1) is invariant

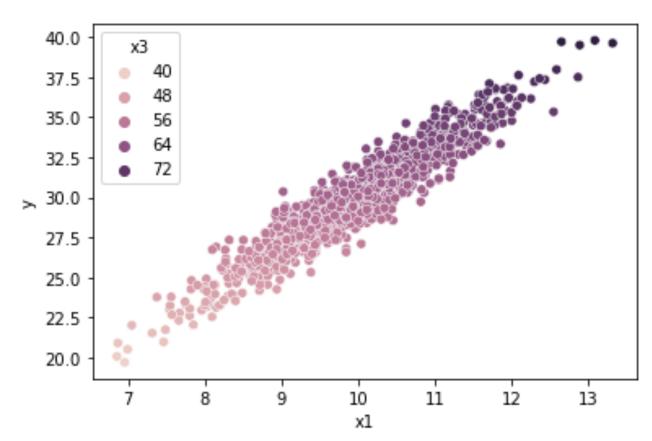


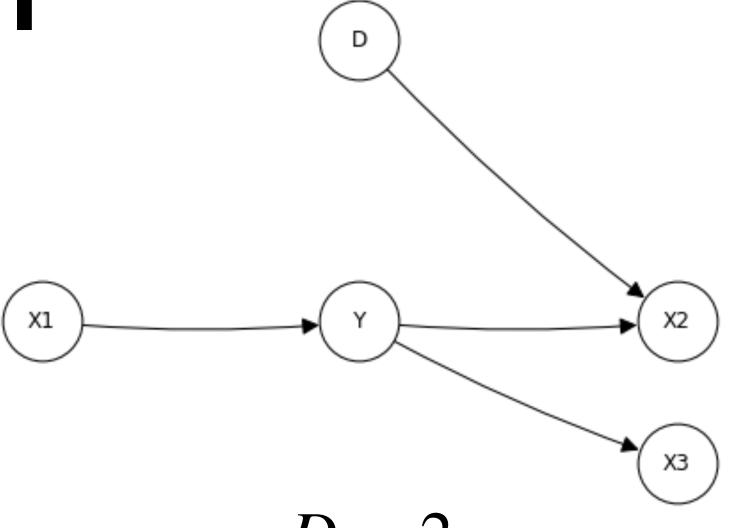
х3	x2	У	x1	d
52.330948	-51.648475	26.130494	8.973763	0
63.802704	-64.373356	31.894998	10.428340	0
50.279162	-52.313502	25.166962	8.911484	0
59.539914	-60.419296	29.783299	9.841798	0
55.327185	-55.075839	27.660573	8.969118	0



D = 1

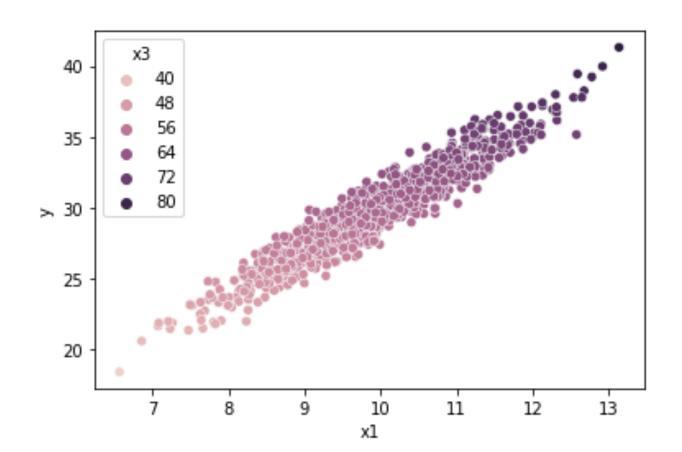
d	x1	у	х2	х3
1	9.941015	28.696601	1	57.475345
1	8.762380	25.715927	1	51.275390
1	9.636201	28.407387	1	56.884332
1	10.875069	31.370200	1	62.686789
1	10.023968	31.253540	1	62.388444



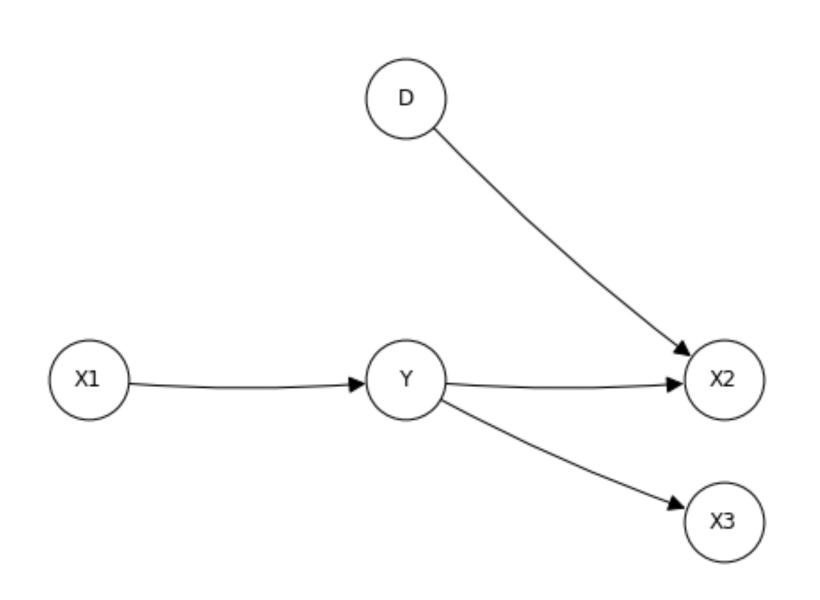


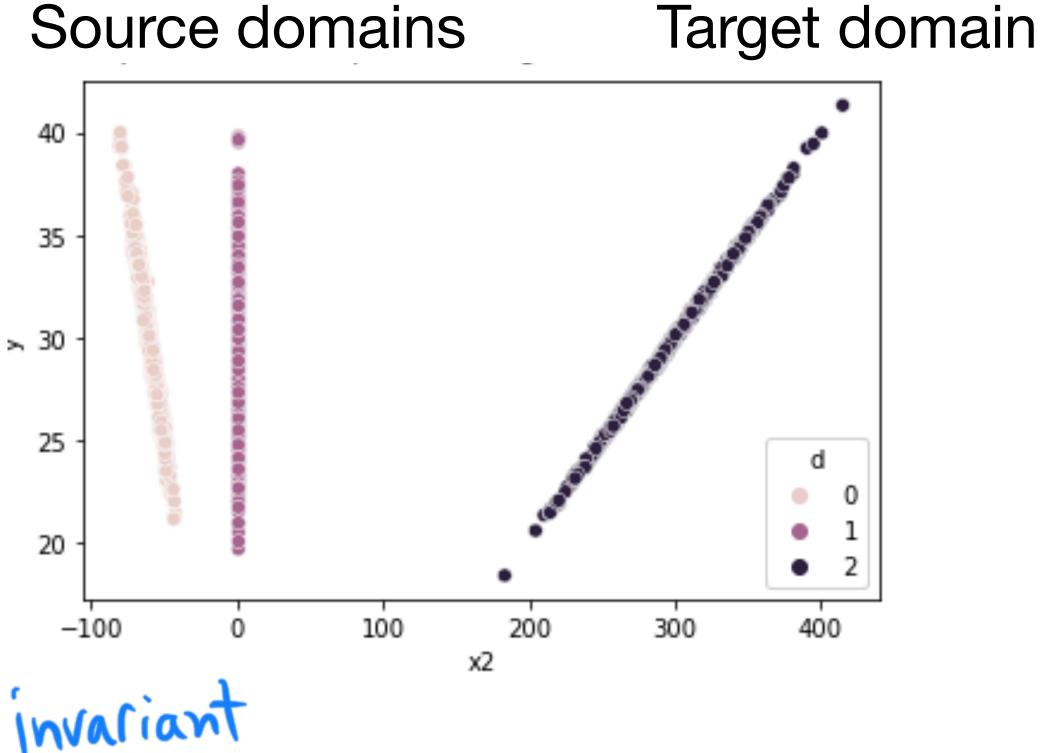
	L

d	x1	У	x2	х3
2	9.671277	26.556214	265.034283	53.338139
2	9.613139	27.120226	270.746784	54.340341
2	10.718335	29.589532	295.318526	59.291053
2	9.002388	26.629254	264.942583	53.340389
2	9.289340	29.030355	289.747562	58.098312



Domain adaptation example - X2



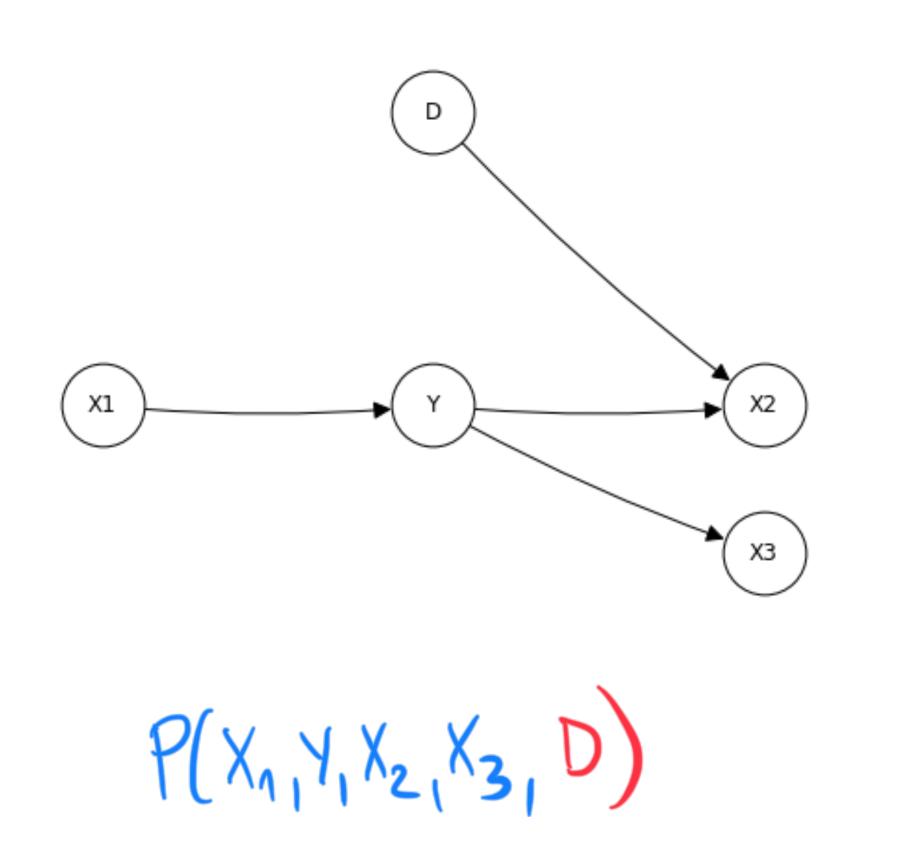


```
P(4/X2) is not invariant
```

```
sns.scatterplot(data = df, x="x2", y="y", hue="d")
X2_0 = df_0["x2"].values.reshape(-1, 1)
X2_2 = df_2["x2"].values.reshape(-1, 1)
model = LinearRegression().fit(X2_0, Y_0)
est_Y_2 = model.predict(X2_2)
print("Mean squared error predicting Y in environment 2 based on model learnt in environment 0 from X2", mean_squared_error(Y_2,est_Y_2))
```

Mean squared error predicting Y in environment 2 based on model learnt in environment 0 from X2 30518.374428658524

Separating features intuition - X1



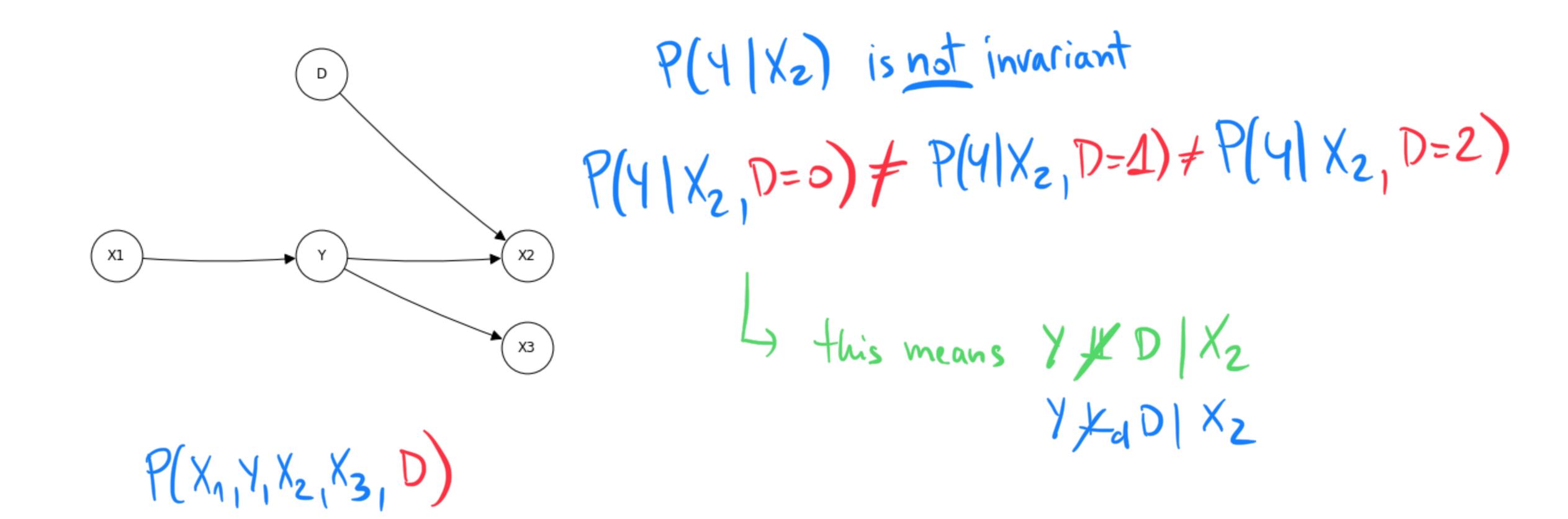
$$P(Y|X_1)$$
 is invariant

 $P(Y|X_1,D=0) = P(Y|X_1,D=1) = P(Y|X_1,D=2)$
 $= P(Y|X_1)$

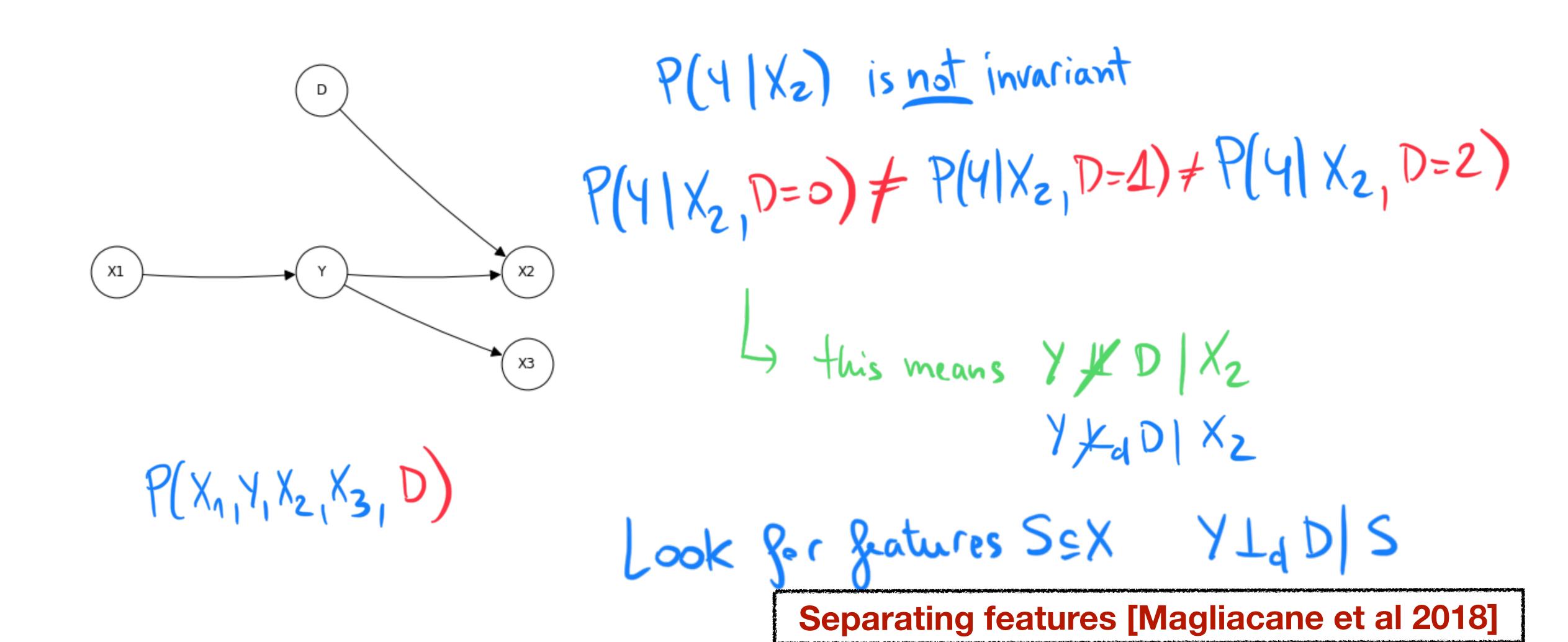
Ly this is the if $Y \perp D \mid X_1$
 $Y \perp D \mid X_1$ in true graph

d-separation [Pearl 1988]

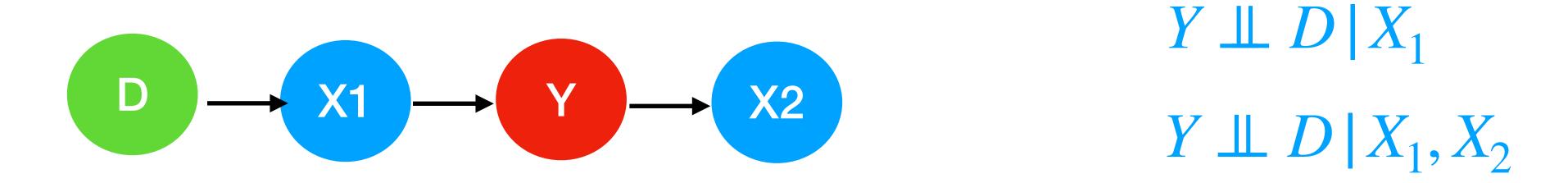
Separating features intuition - X2



Separating features intuition - X2

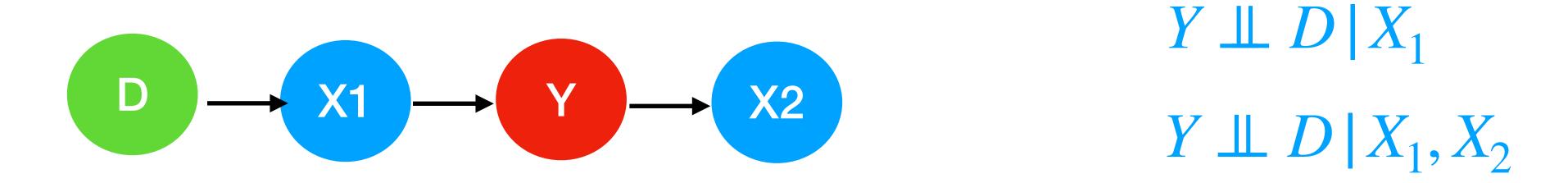


Common misconceptions: 1. An invariant feature need not be causal



• Y|X1,X2 is invariant \Longrightarrow invariant features are not necessarily parents of Y

Common misconceptions: 1. An invariant feature need not be causal



• Y|X1,X2 is invariant \Longrightarrow invariant features are not necessarily parents of Y

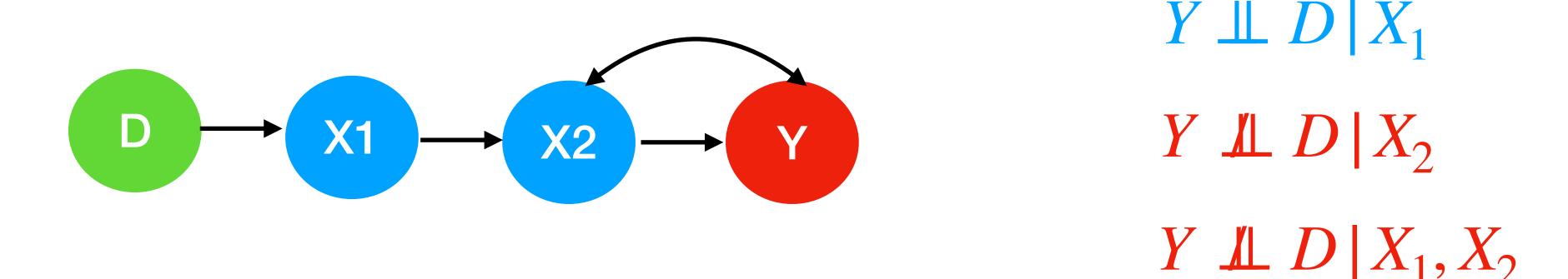
Invariant feature across "many different datasets" is not enough in general to find causal parents, need more assumptions

Common misconceptions: 1. An invariant feature need not be causal

- Y|X1,X2 is invariant \Longrightarrow invariant features are not necessarily parents of Y|X1,X2
- Invariant Causal Prediction [Peters et al. 2016] under causal sufficiency:

$$\mathbf{S}^* = \bigcap_{Y \sqcup D \mid \mathbf{S}} \mathbf{S} \subseteq Pa(Y) \qquad \{X_1, X_2\} \cap \{X_1\} = \{X_1\}$$

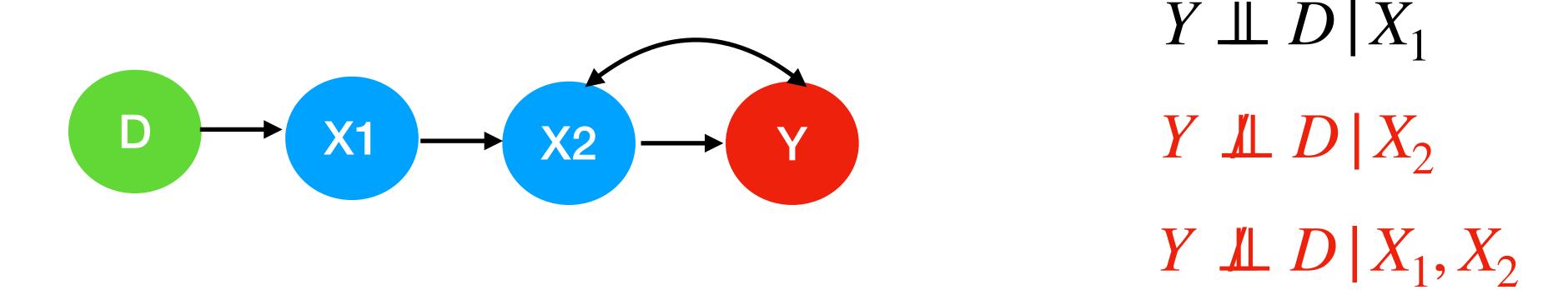
Common misconception 2: Parents are not enough under latent confounding



• YX1 is invariant, YX2 is not

Even if we knew all the parents, under latent confounding this wouldn't necessarily help transfer

Common misconception 2: Parents are not enough under latent confounding



Y|X1 is invariant, Y|X2 is not

Even if we knew all the parents, under latent confounding this wouldn't necessarily help transfer

• Conclusion: causality (e.g. using the causal parents, learning the complete causal graph) is neither necessary or sufficient* for transfer

Desiderata for a causality inspired domain adaptation method

- X, Y and changes can be represented by an unknown causal graph
- Allow for latent confounders
- Avoid parametric assumptions, allow for heterogeneous effects across domains

Desiderata for a causality inspired domain adaptation method

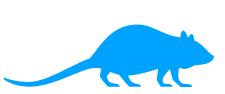
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Desiderata for a causality inspired domain adaptation method

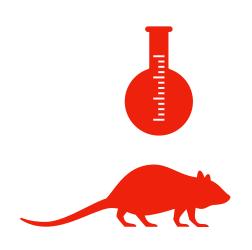
- X, Y and changes can be represented by an unknown causal graph
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- Instead of modeling changes between each domain, distinguish the change between the mixture of sources and the target
- Avoid common assumption that if Y T(X) is invariant across multiple source domains, then Y T(X) is invariant also in the target domain
 - This also (implicitly) assumed by methods based on the idea that invariance => causality

Causal domain adaptation problem [Magliacane et al. 2018]

- Unsupervised multi-source domain adaptation
- We interpret the change in the target domain as a soft intervention
- We assume Y cannot be intervened upon directly P(Y) can still change

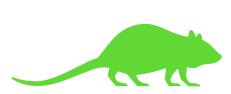


	X1	X2	Y
Normal	0.1	2	0
Normal	0.2	3	0
Normal	1.1	2	1
Normal	0.1	3	0



	X1	X2	Y
Gene B	0.2	1	?
Gene B	0.3	1	?
Gene B	0.3	2	?
Gene B	0.4	1	?

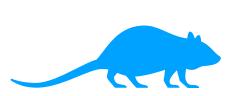




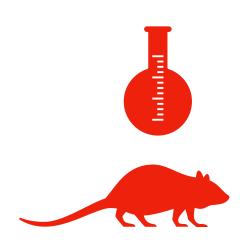
Causal domain adaptation [Magliacane et al. 2018]

Multiple context variable C1, C2 ...

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- We interpret the change in the target domain as a soft intervention
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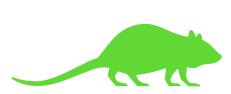


	X1	X2	Y
Normal	0.1	2	0
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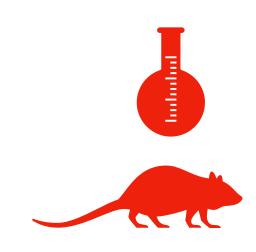


Causal domain adaptation problem [Magliacane et al. 2018]

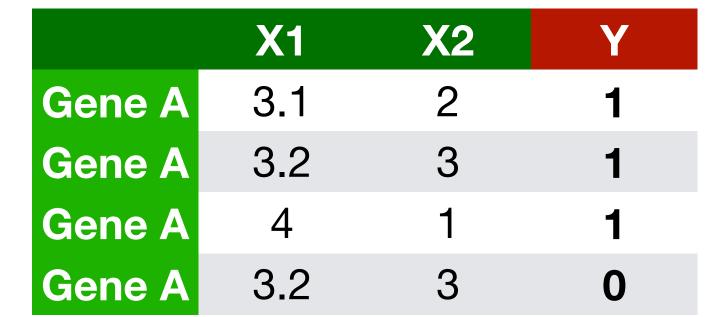
- Unsupervised multi-source domain adap
 C1 = 1
- We interpret the change in the target domain as a soft intervention
- We assume Y cannot be intervened upon directly P(Y) can still change



	X1	X2	Y
Normal	0.1	2	0
Normal	0.2	3	0
Normal	1.1	2	1
Normal	0.1	3	0



	X1	X2	Y
Gene B	0.2	1	?
Gene B	0.3	1	?
Gene B	0.3	2	?
Gene B	0.4	1	?





Causal domain adaptation problem [Magliacane et al. 2018]

- Unsupervised multi-source domain adaptation
- We interpret the change in the target domain as a soft intervention
- We assume Y cannot be intervened upon directly P(Y) can still change



	X1	X2	Y
Normal	0.1	2	0
Normal	0.2	3	0
Normal	1.1	2	1
Normal	0.1	3	0

	X1	X2	Y
Gene A	3.1	2	1
Gene A	3.2	3	1
Gene A	4	1	1
Gene A	3.2	3	0





Joint Causal Inference [Mooij et al. 2020]

- We represent jointly different distributions as an unknown single causal graph
- Instead of a single domain variable, we add several context variables so we can disentangle changes in distribution across the datasets
 - If we know nothing about the changes in the datasets, we use indicator variables

_								
				X1		X2		Y
	Norr	nal		0.1		2		0
	Norr	nal		0.2		3		0
			X 1		X2		V	1
Ger	ne A		3.1		2		1	
	ne A		3.2		3		1	
	- A	V	1	V _O	1		1	
		<u>X1</u>		X2		Y		
Gene I	В	0.2		1		?		
Gene l	В	0.3		1		?		
Gene l	В	0.3		2		?		
Gene I	В	0.4		1		?		

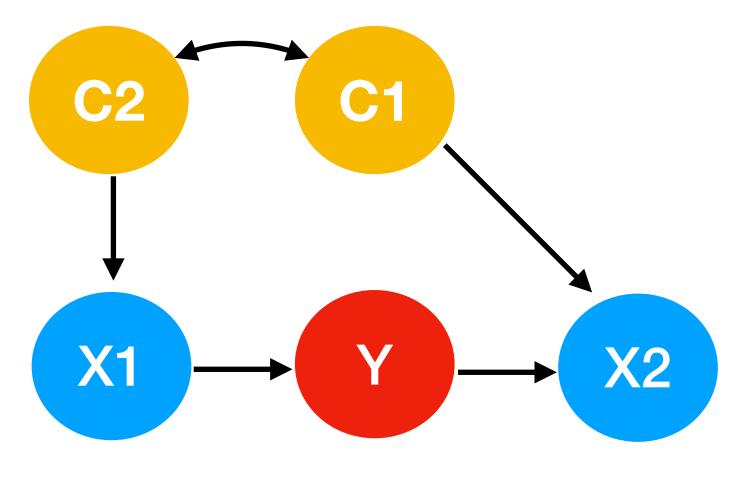
C1	C2	X1	X2	Y
0	0	0.1	2	0
0	0	0.2	3	0
0	0	1.1	2	1
0	0	0.1	3	0
1	0	3.1	2	1
1	0	3.2	3	1
1	0	4	1	1
1	0	3.2	3	0
0	1	0.2	1	?
0	1	0.3	1	?
0	1	0.3	2	?
0	1	0.4	1	?

Joint Causal Inference [Mooij et al. 2020]

- We can learn an equivalence class of the unknown single causal graph using conditional independence tests on systematically pooled data
- We treat context variables as normal variables that we know are uncaused

C1	C2	X1	X2	Y
0	0	0.1	1	0
0	0	0.2	1	0
0	0	1.1	2	1
1	0	3.1	2	1
1	0	3.2	3	1
1	0	4	3	1
0	1	0.2	0	0
0	1	0.3	0	1
0	1	0.3	1	0

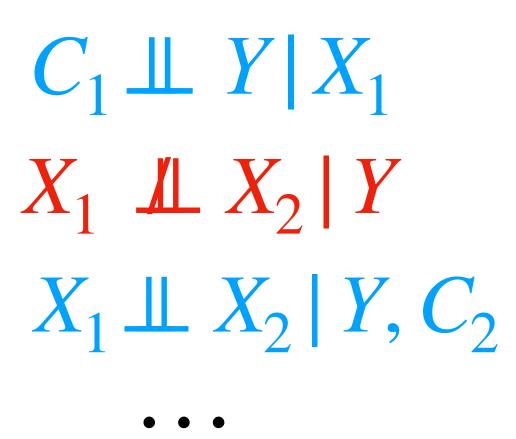
$$C_1 \perp \!\!\! \perp \!\!\! \mid Y \mid X_1$$
 $X_1 \perp \!\!\! \perp \!\!\! \mid X_2 \mid Y$
 $X_1 \perp \!\!\! \perp \!\!\! \perp X_2 \mid Y, C_2$

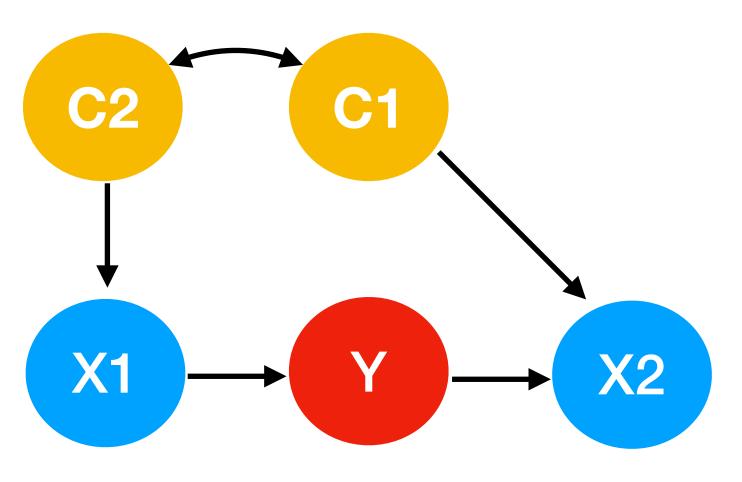


Joint Causal Inference [Mooij et al. 2020]

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C1	C2	X1	X2	Y
0	0	0.1	1	0
0	0	0.2	1	0
0	0	1.1	2	1
1	0	3.1	2	1
1	0	3.2	3	1
1	0	4	3	1
0	1	0.2	0	0
0	1	0.3	0	1
0	1	0.3	1	0



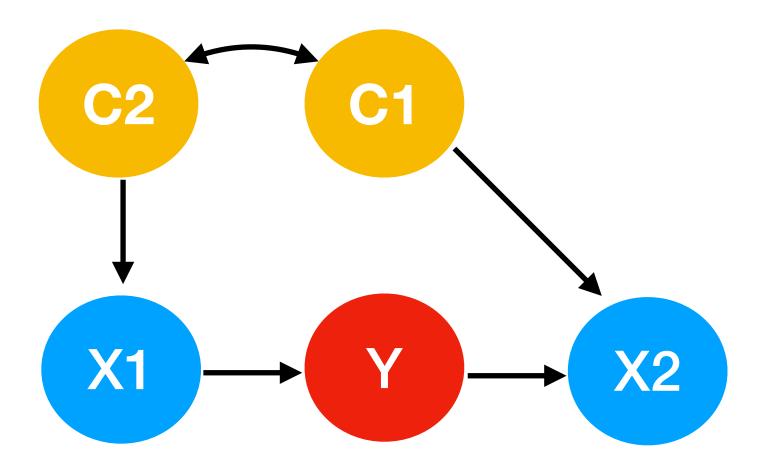


Causal domain adaptation: separating features

• Separating features: sets of features that d-separate Y from the context

variable C1 representing the target domain

Aka stable features, invariant features etc.



• {X1} is a separating feature set, {X1, X2} could lead to arbitrary large error

Idea: we could test the conditional independence in the data

$$Y \perp \!\!\! \perp C_1 \mid X_1? \qquad Y \perp \!\!\! \perp C_1 \mid X_2?$$

Idea: we could test the conditional independence in the data

• Problem: Y is always missing when C1=1, so we cannot test these

C1	C2	X1	X2	Y
0	0	0.1	1	0
0	0	0.2	1	0
0	0	1.1	2	1
1	0	3.1	2	?
1	0	3.2	3	?
1	0	4	3	?
0	1	0.2	0	0
0	1	0.3	0	1
0	1	0.3	1	0

• Idea: we could test the conditional independence in the data

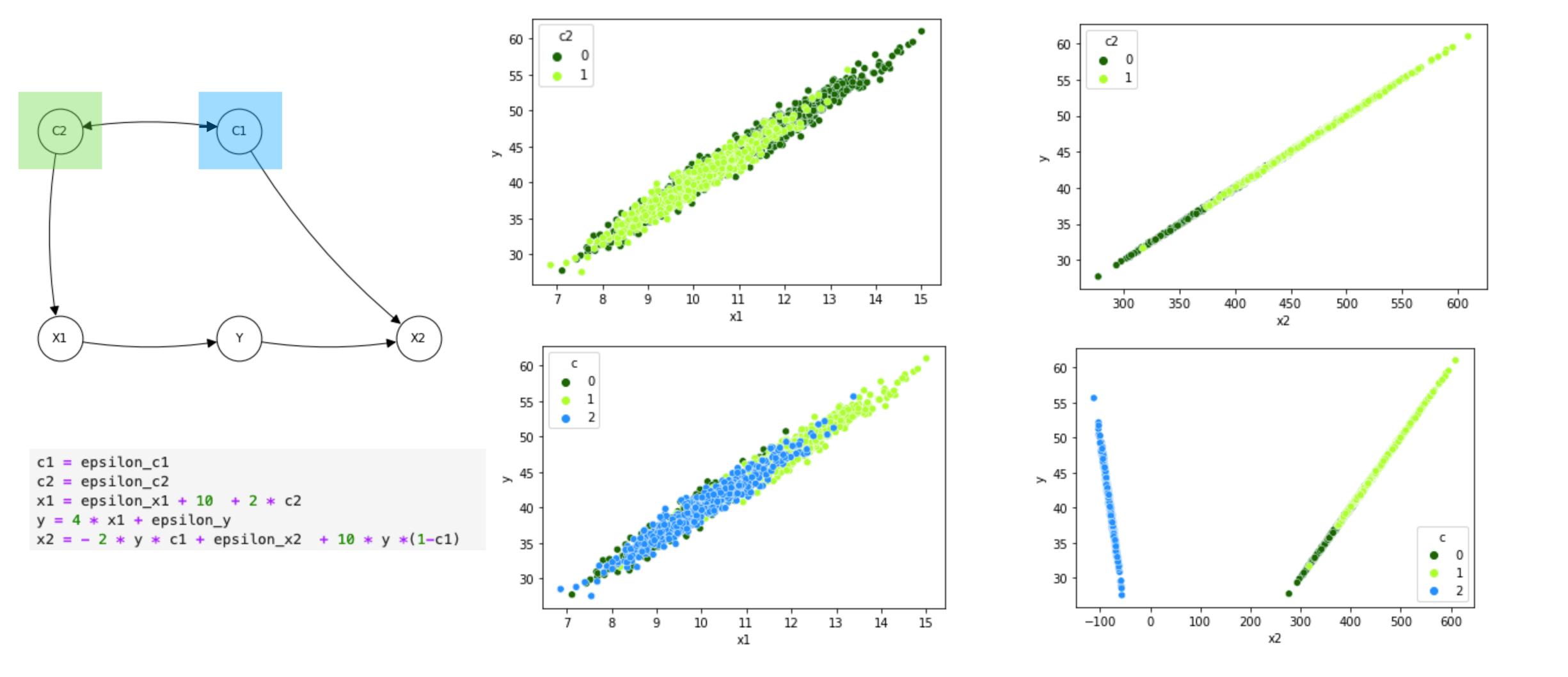
Problem: Y is always missing when C1=1, so we cannot test these

C1	C2	X1	X2	Y
0	0	0.1	1	0
0	0	0.2	1	0
0	0	1.1	2	1
1	0	3.1	2	?
1	0	3.2	3	?
1	0	4	3	?
0	1	0.2	0	0
0	1	0.3	0	1
0	1	0.3	1	0

Idea: Separating features in sources are also separating in target

$$Y \perp \!\!\! \perp C_2 \mid X_1 \implies Y \perp \!\!\! \perp C_1 \mid X_1$$

Separating features in sources are also separating in target - counterexample



Idea: we could test the conditional independence in the data

• **Problem:** Y is always missing when C1=1, so we cannot test these

C1	C2	X1	X2	Y
0	0	0.1	1	0
0	0	0.2	1	0
0	0	1.1	2	1
1	0	3.1	2	?
1	0	3.2	3	?
1	0	4	3	?
0	1	0.2	0	0
0	1	0.3	0	1
0	1	0.3	1	0

$$X_{1} \perp X_{2}$$
 $X_{1} \perp C_{1}$
 $X_{1} \perp X_{2} \mid C_{1}$
 $X_{1} \perp X_{2} \mid C_{1}$
 $X_{1} \perp X_{2} \mid Y, C_{1} = 0$

• Idea: Can we use all other in/dependences?

Assumptions [Magliacane et al. 2018]

- We assume that there exists an acyclic causal graph that fits all the data (Joint Causal Inference)
- We assume Y cannot be intervened upon directly

Assumptions [Magliacane et al. 2018]

- We assume that there exists an acyclic causal graph that fits all the data (Joint Causal Inference)
- We assume Y cannot be intervened upon directly
- We assume no extra dependences involving Y in target domain C1=1

$$A, D, \mathbf{B} \subset \mathbf{V} \setminus \{Y, C_1\}$$
 $Y \perp \!\!\!\perp A \mid \mathbf{B}, C_1 = 0 \implies Y \perp \!\!\!\perp A \mid \mathbf{B}, C_1 = 1$
 $A \perp \!\!\!\perp D \mid \mathbf{B}, Y, C_1 = 0 \implies A \perp \!\!\!\perp D \mid \mathbf{B}, Y, C_1 = 1$

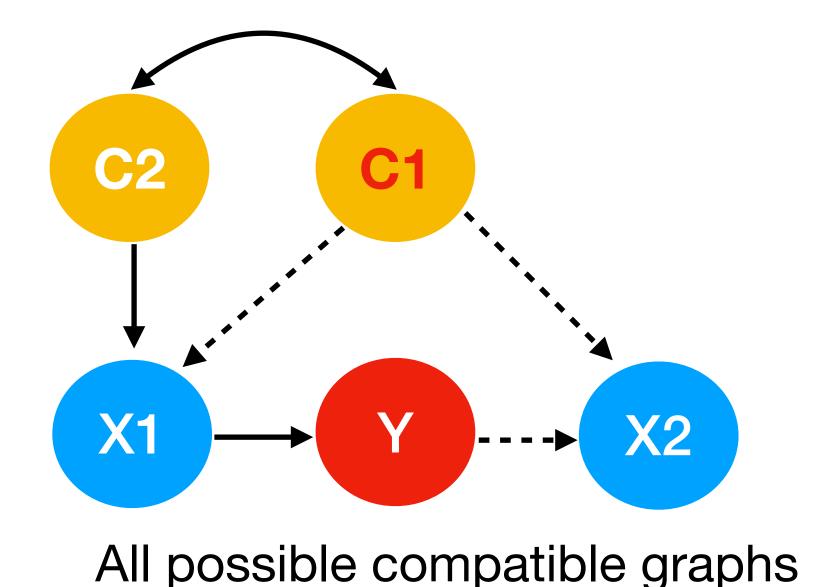
There can be extra independences in the target

A simple example

C1	C2	X1	X2	Y
0	0	0.1	1	0
0	0	0.2	1	0
0	0	1.1	2	1
0	1	3.1	2	1
0	1	3.2	3	1
0	1	4	3	1
1	0	0.2	0	?
1	0	0.3	0	?
1	0	0.3	1	?

$$Y \perp \!\!\! \perp C_2 \mid C_1 = 0$$
 $Y \perp \!\!\! \perp C_2 \mid X_1, C_1 = 0$
 $X_2 \perp \!\!\! \perp C_2 \mid Y, C_1 = 0$

Perform allowed CI tests

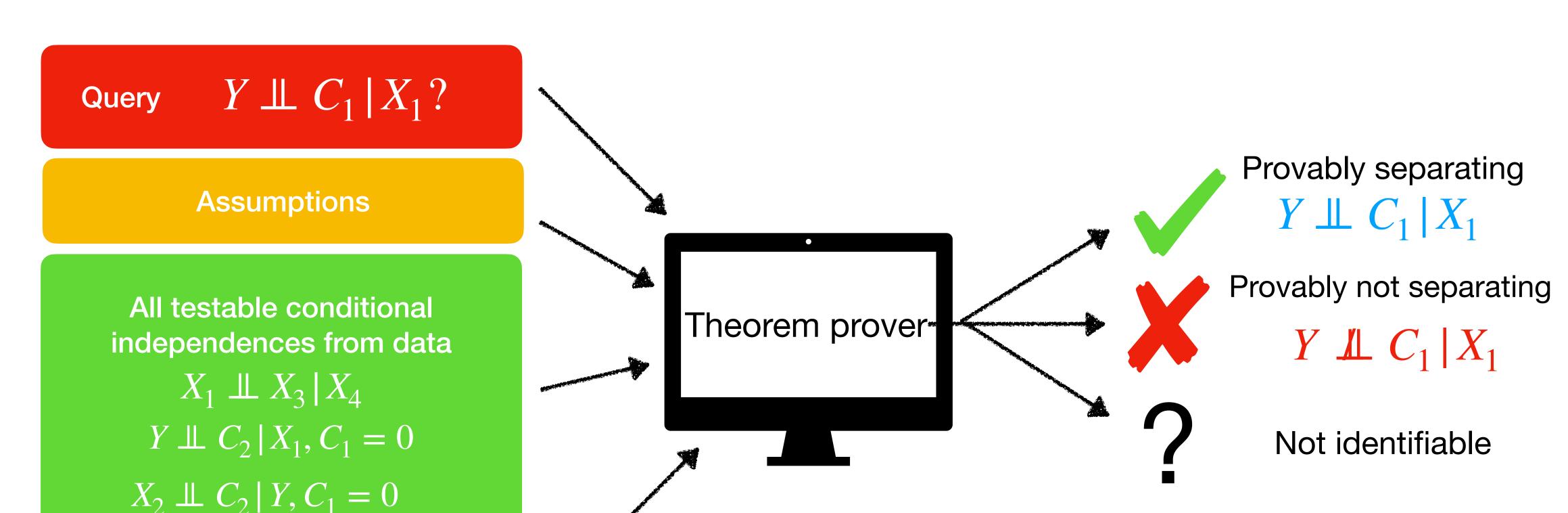


We can prove untestable separating test without reconstructing the graph:

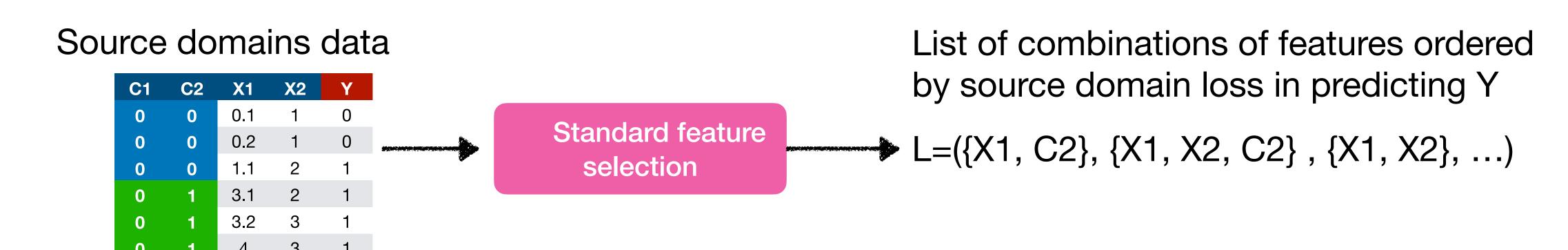
$$Y \perp \!\!\! \perp C_1 \mid X_1$$

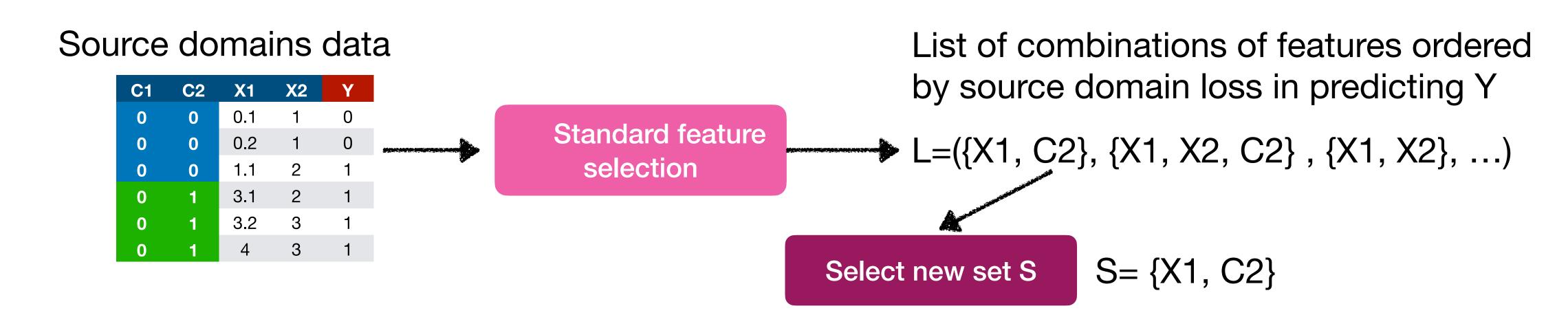
True in all possible compatible graphs

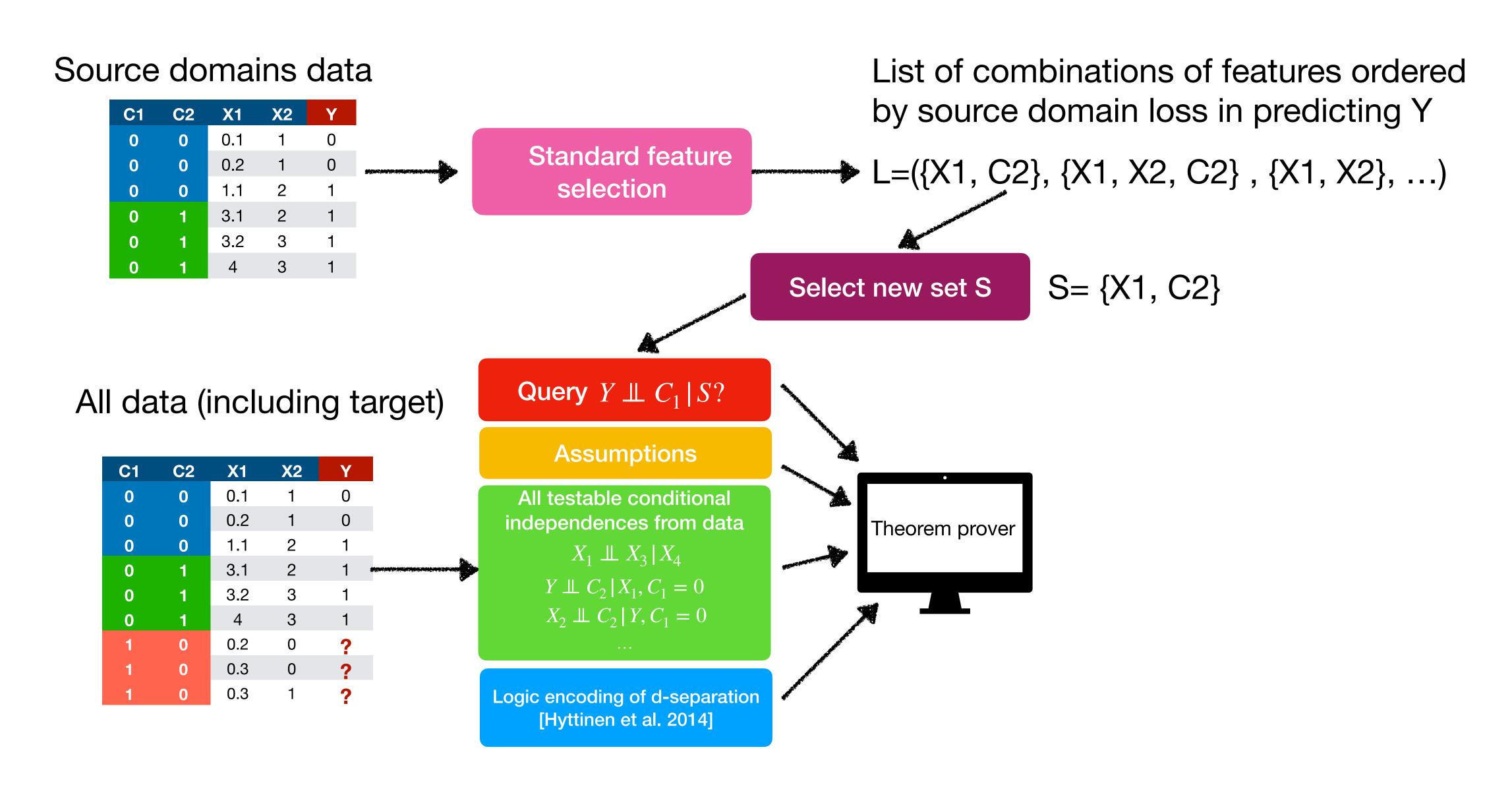
Inferring separating sets without enumerating all possible causal graphs

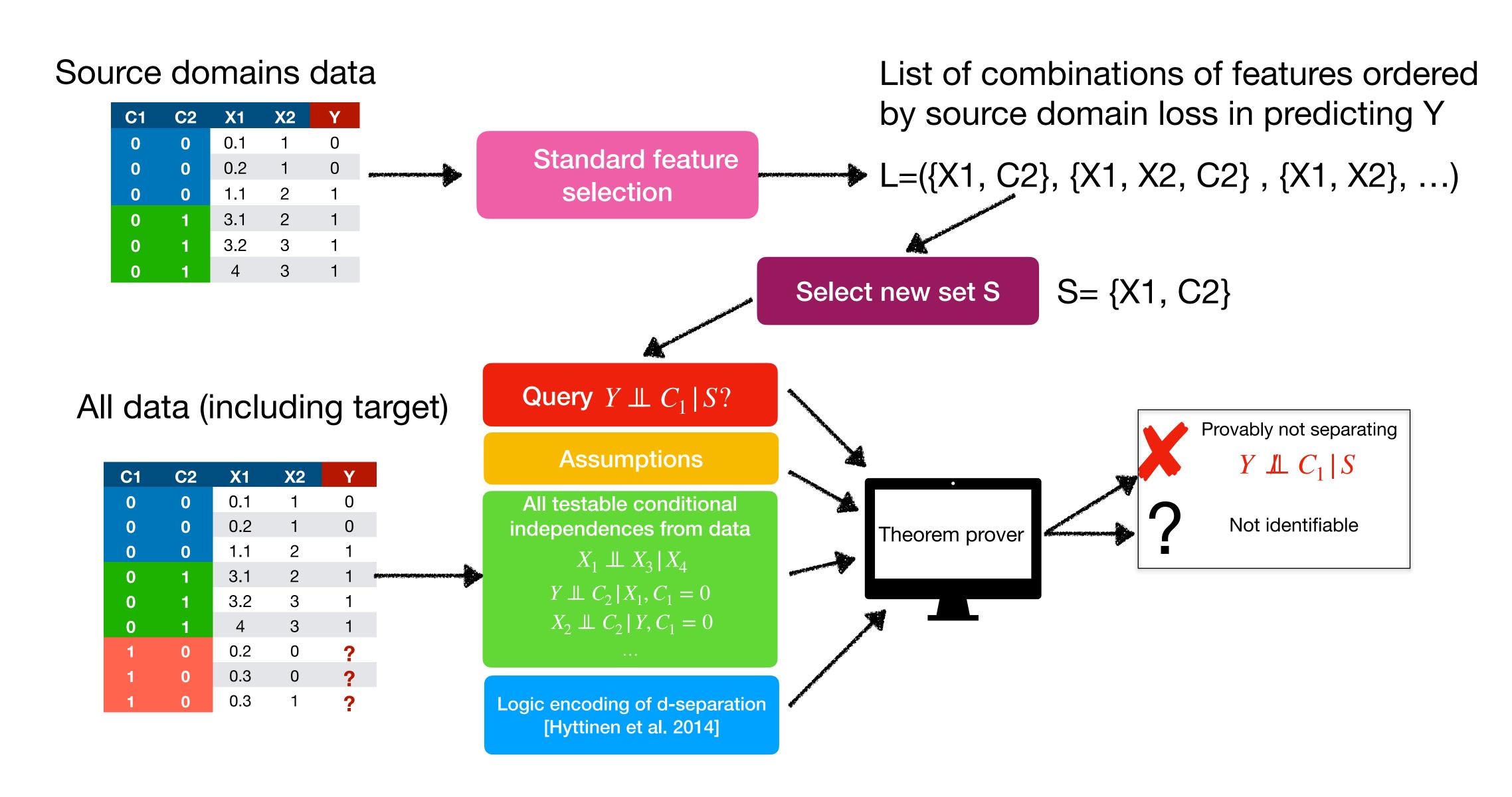


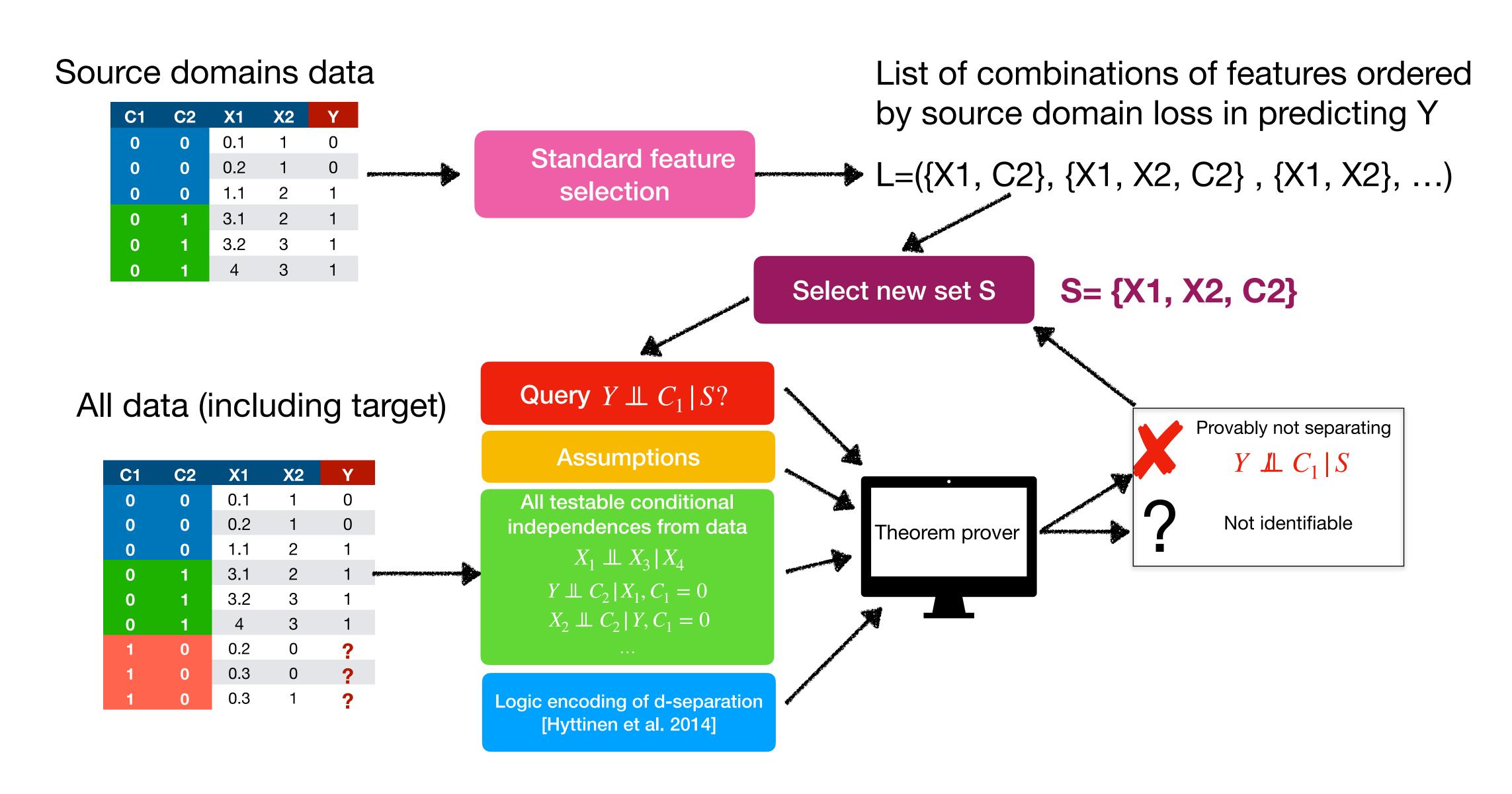
Logic encoding of d-separation [Hyttinen et al. 2014]

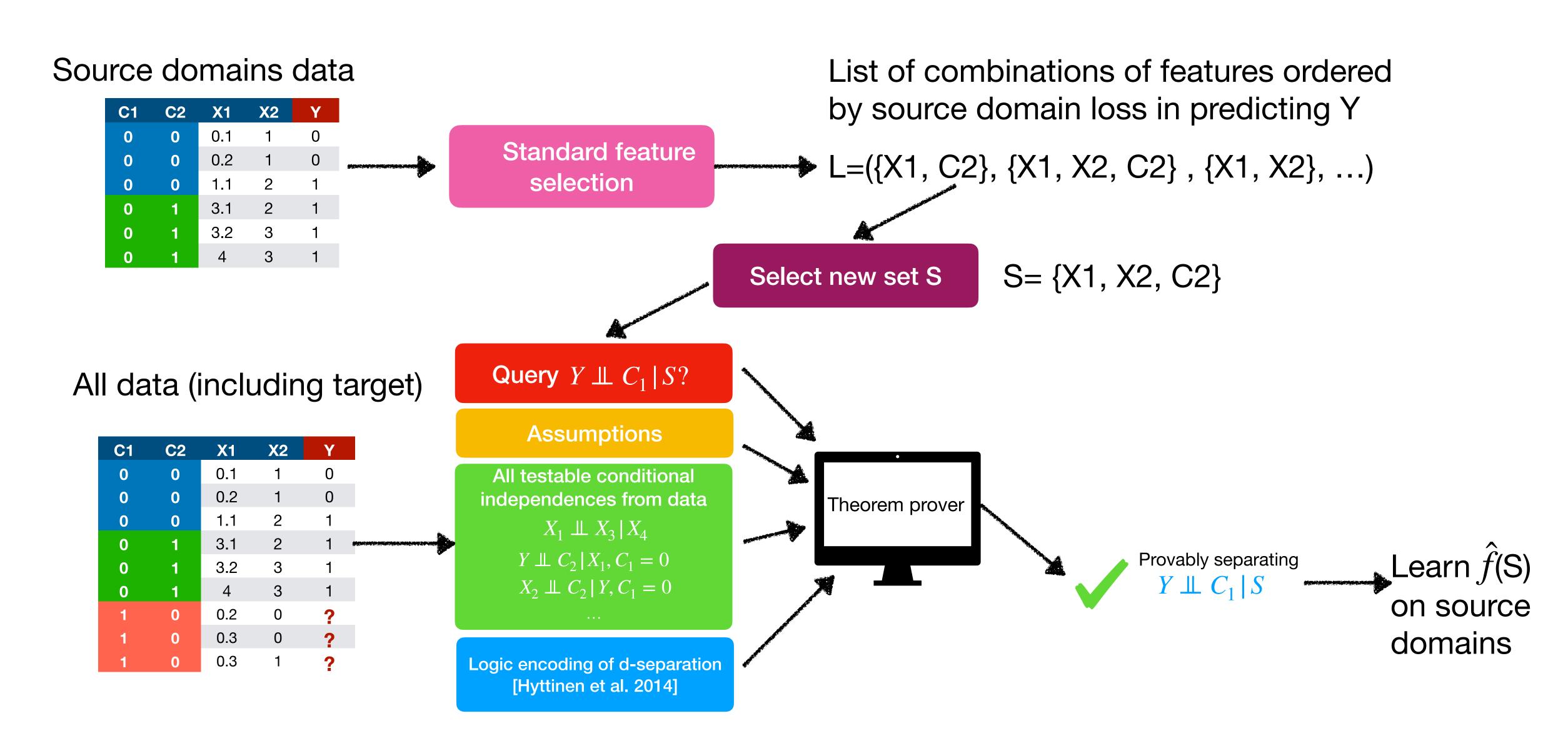


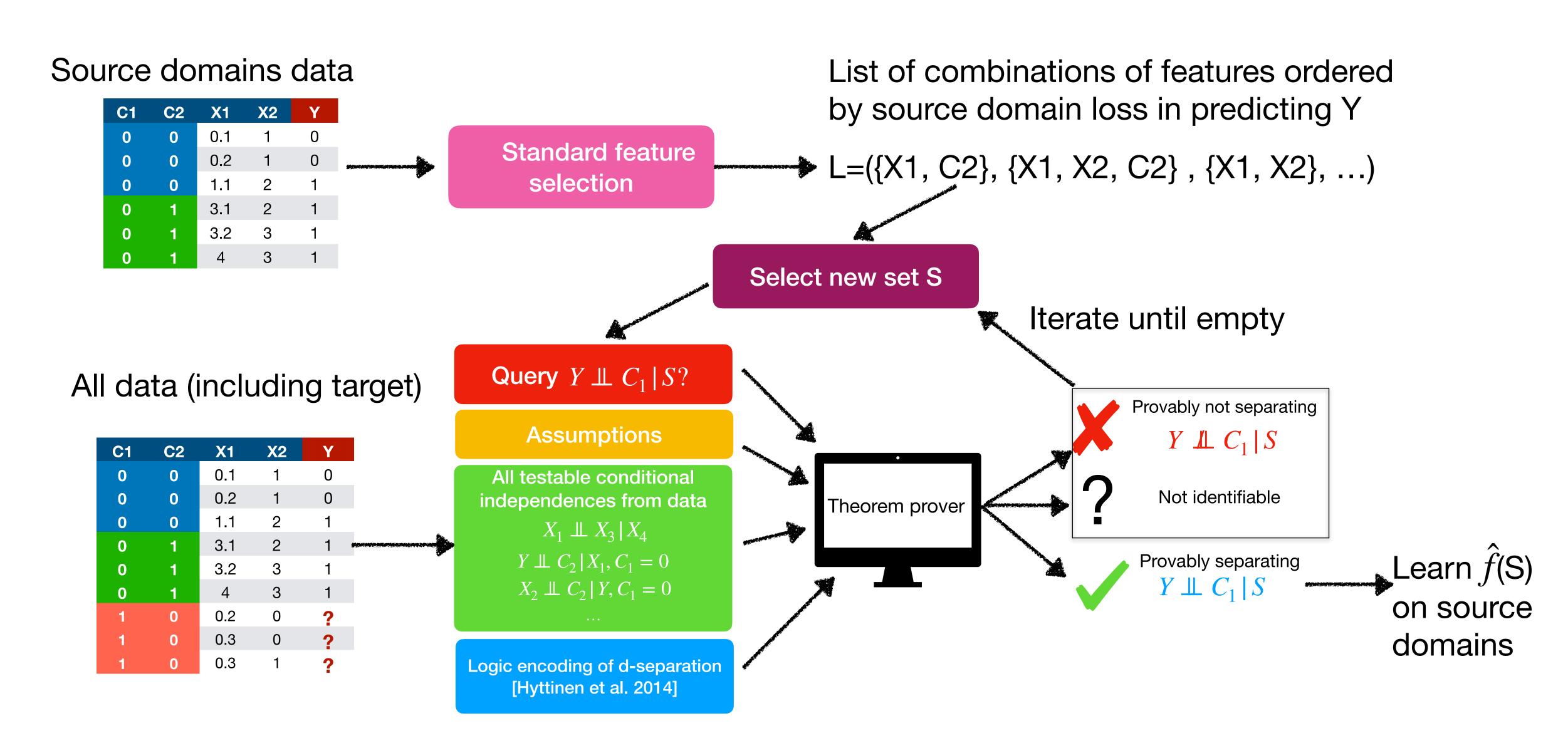


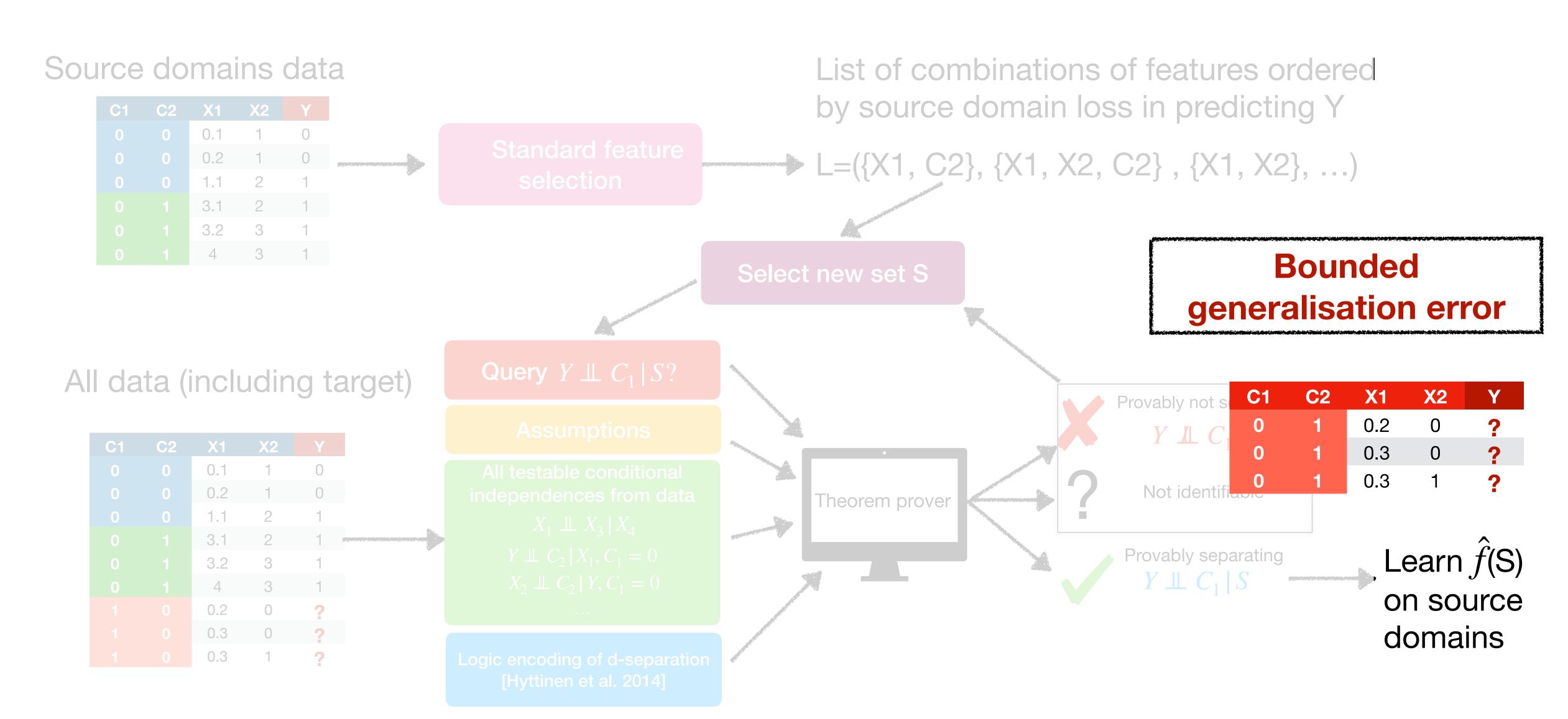












Desiderata for a causality inspired domain adaptation method



Thanks to JCI
[Mooij et al 2020]

- Allow for latent confounders
- Avoid parametric assumptions, allow for heterogeneous effects across domains
- Instead of modeling changes between each domain, distinguish the change between the mixture of sources and the target
- Avoid common assumption that if Y| T(X) is invariant across multiple source domains, then Y|T(X) is invariant also in the target domain
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no need to find causal graph or equivalence class

Limitations and future work

- Potentially too conservative: Separating sets may exist that are not provably separating
 - Extension: can we use active learning/intervention design to decide most informative interventions?
- Scalability: using (error-correcting) logic-based encoding with all CI tests as input scales to tens of vars (including context variables)
 - Extension: use approximate algorithms, combine with low dim representations
- Can we apply this to multi-task RL (e.g. in factored MDPs)?

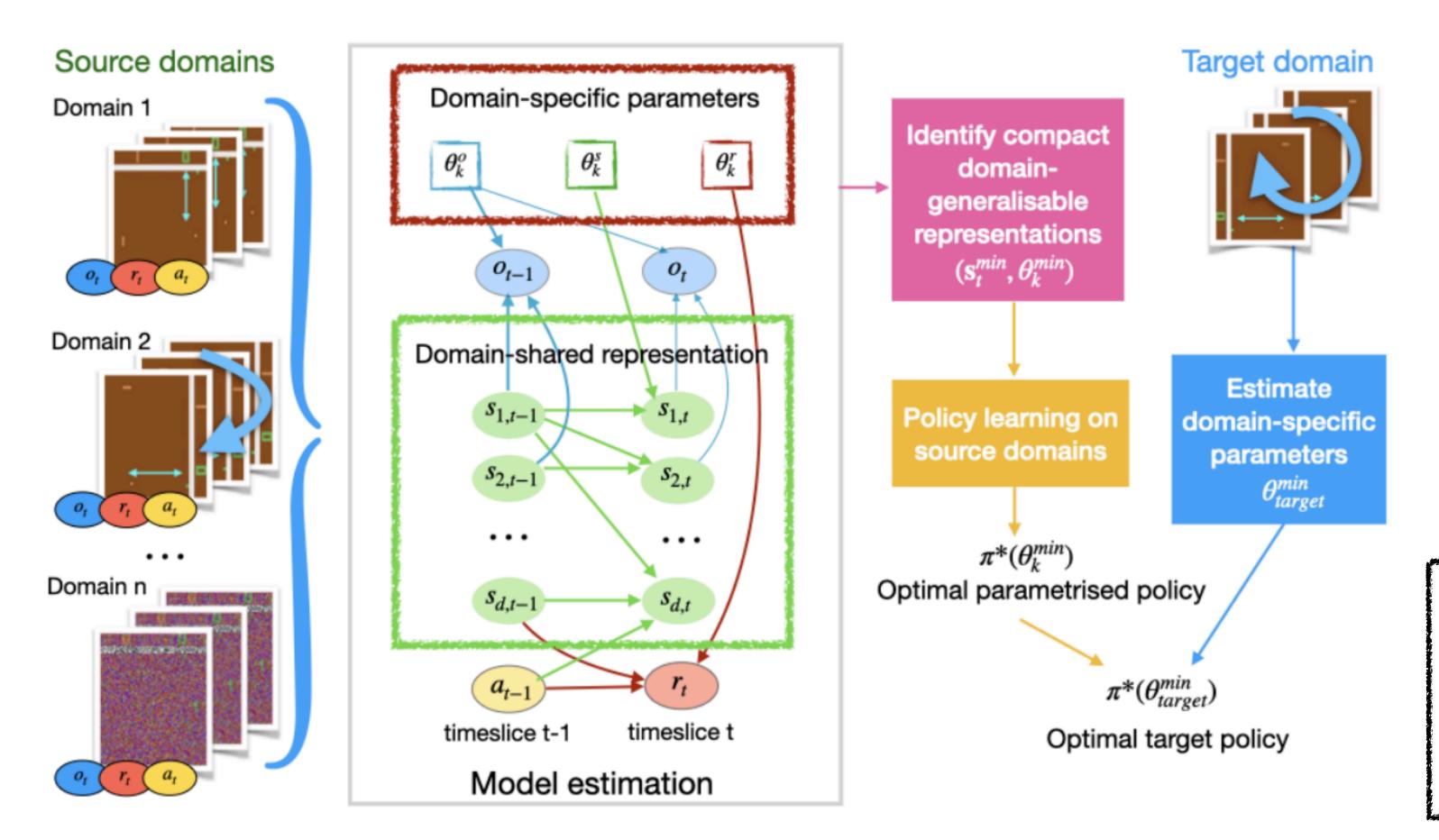
AdaRL: What, Where, and How to Adapt in Transfer RL

Biwei Huang, Fan Feng, Chaochao Lu, Sara Magliacane, Kun Zhang

- We have n source domains with random trajectories
- Learn a factored MDP (symbolic inputs) or POMDP (images) with latent change factors that are constant in each domain, but vary across domains over sources
 - Identify the minimal dimensions of the state and change factors that are necessary and sufficient for policy optimisation
- Learn a policy over all source domains, parametrised in the minimal change factors
- In the target domain learn the value of the change factor and apply this policy

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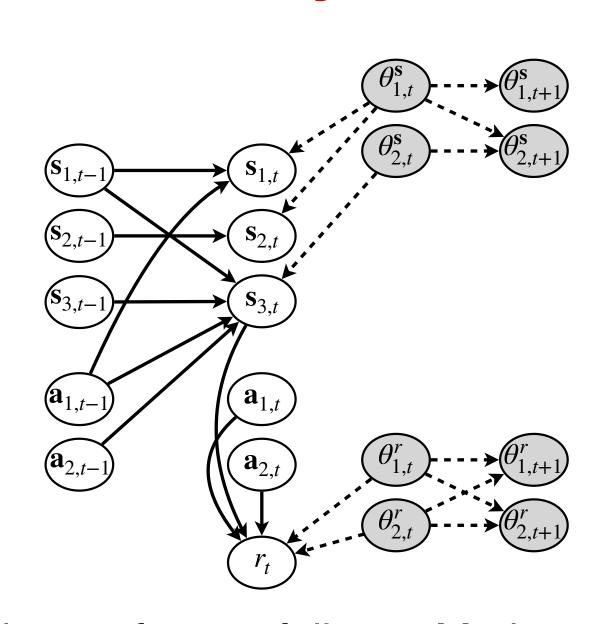


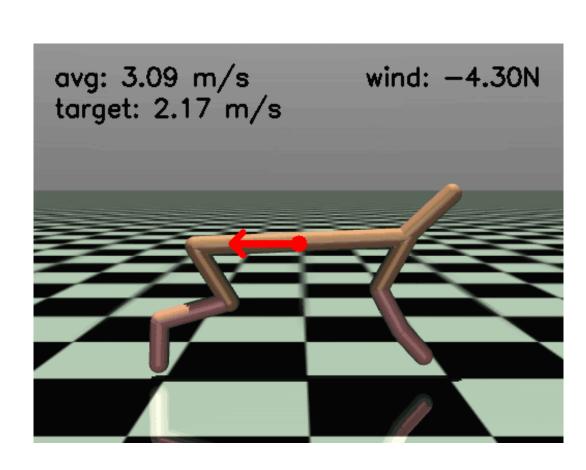
Simplifying assumption: no new edges in target domain

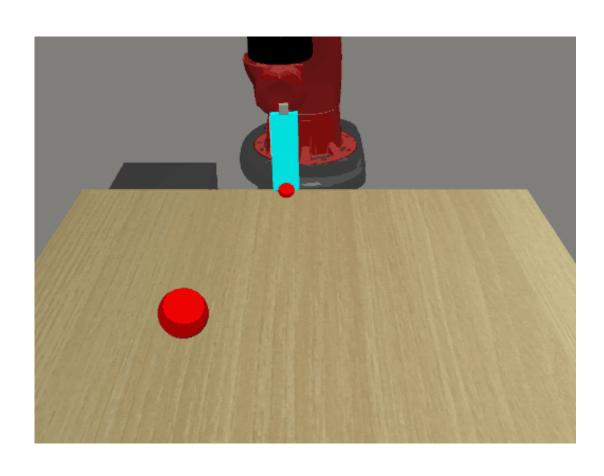
FansRL: Factored Adaptation for Non-Stationary Reinforcement Learning

Fan Feng, Biwei Huang, Kun Zhang, Sara Magliacane

 The latent change factors are not constant anymore and they model nonstationarity







Change factors follow a Markov process:

Non-stationary environments (wind changes)

Non-stationary rewards (target changes)

- Discrete/abrupt changes
- Continuous/smooth changes

Conclusions

- D-separation [Pearl 1988] is a principled way to reason about invariances and distribution shift
 - Not a new observation, known since [Schoelkopf et al 2012, Zhang et al. 2013]
 - This is true even with:
 - Unknown causal graph
 - Missing data/CI (so unknown MEC)
- D-separation logic encodings [Hyttinen et al 2014] allow us to reason about d-separations even with missing data, even without reconstructing MEC

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Thanks! Questions?

(joint work with Thijs van Ommen, Tom Claassen, Stephan Bongers, Philip Versteeg, Joris Mooij, Biwei Huang, Fan Feng, Chaochao Lu and Kun Zhang)